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# Optical constants and roughness study of dc magnetron sputtered iridium films

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Extremely smooth thin films of iridium have been deposited onto superpolished fused silica substrates using dc magnetron sputtering in an argon plasma. The influence of deposition process parameters on film microroughness has been investigated. In addition, film optical constants have been determined using variable angle spectroscopic ellipsometry, over the spectral range from vacuum ultraviolet to middle infrared (140 nm–35  $\mu$ m). Because the Ir films were optically thick and the surface roughnesses were measured by atomic force microscopy then accounted for in the optical model, the as-determined film optical constants are expected to be the best available for Ir bulk metals, minimally affected by surface overlayers or microstructure. © 2002 American Institute of Physics. [DOI: 10.1063/1.1509091]

## I. INTRODUCTION

The need for durable, corrosion-free, reproducible iridium (Ir) thin films with a smooth surface and good adhesion to substrates has drawn considerable attention recently for various applications.<sup>1,2</sup> Ir is of great interest because of its unique properties, including a high melting point ( $\sim 2713$  K), low oxygen permeability, high chemical stability, and good electric conductivity, to name a few.<sup>1–4</sup> As a result, it is currently being considered by NASA as a substrate (Ir on fused silica) for use in space contamination studies.<sup>5,6</sup> For use in space, Ir films with excellent surface qualities are necessary, including extremely low surface roughness and superb stability in the adverse environment in space.

Various deposition techniques have been employed to prepare Ir films, including metalorganic chemical vapor deposition (CVD),<sup>7–9</sup> CVD,<sup>10</sup> dc, and rf magnetron sputtering.<sup>1–3,11</sup> Due to the strong influence of morphology on film properties, film microstructure is an important property to consider for both optical and microelectronic applications. Moreover, environmental stability depends strongly on film morphology as well. Surface roughness of sputtered Ir metal films is, to a great extent, induced by the surface roughness of the substrate and the microstructure of the coatings. Superpolished fused silica (amorphous) was used as the substrate in our study to minimize the effects of surface roughness.

Magnetron sputtering is currently the most widely commercially practiced sputtering method.<sup>12</sup> It features a high sputtering rate at the target, high deposition rate, and superior adhesion of sputtered films.<sup>13,14</sup> In the present study, Ir films with smooth surfaces were prepared by dc magnetron sputtering. The effects of processing parameters, including gas pressure in the deposition chamber, deposition duration, etc., on film surface roughness were investigated. In addition,

Ir film optical constants over the spectral range from vacuum ultraviolet (VUV) through middle infrared (MIR) were determined using variable angle spectroscopic ellipsometry (VASE<sup>®</sup>). Previous measurements of Ir optical constants can be found in the literature.<sup>15,16</sup> The present work covers a much wider spectral range and includes atomic force microscopy (AFM) characterization of surface roughness. Optical constants depend on surface roughnesses and oxide growth. Oxygen free Ir films were grown in this study by dc magnetron sputtering, and the smoother the surface the closer are measured optical constants to the true optical constants of the metal.

## II. EXPERIMENT

### A. Film preparation

Ir films were prepared by dc magnetron sputtering in a four-gun cryopumped deposition chamber, as illustrated in Fig. 1. Each of the four guns can be powered separately by either rf or dc source, and eight substrate holders are placed overhead on a temperature controlled rotating platen. The substrate-target spacing is 10 cm.

Commercial fused silica disks (Esco Products Inc.) of 1 in. in diameter and 1/4 in. in thickness were used for this experiment. The disks were subsequently cleaned ultrasonically with acetone and methanol, and then blow-dried with nitrogen gas. The coating target iridium was 99.8% pure, in the form of a disk of 2 in. diameter and 1/8 in. thick. To help the Ir films to better adhere to the fused silica surface, a chromium (Cr) layer of about 24 nm thickness was first deposited as a buffer. Before any deposition, the target (either Cr or Ir) was presputtered for  $\sim 10$  min while keeping the fused silica substrates covered by shutters.

The coating system was cryopumped to  $\sim 5 \times 10^{-7}$  Torr before introducing ultrahigh purity argon (Ar) sputtering gas. Next, Cr layers were deposited with 20 sccm of Ar gas flux flow, at 5 mTorr and 40 W of power, with an approximate deposition rate of 0.2 nm/s. Finally, the Ir depo-

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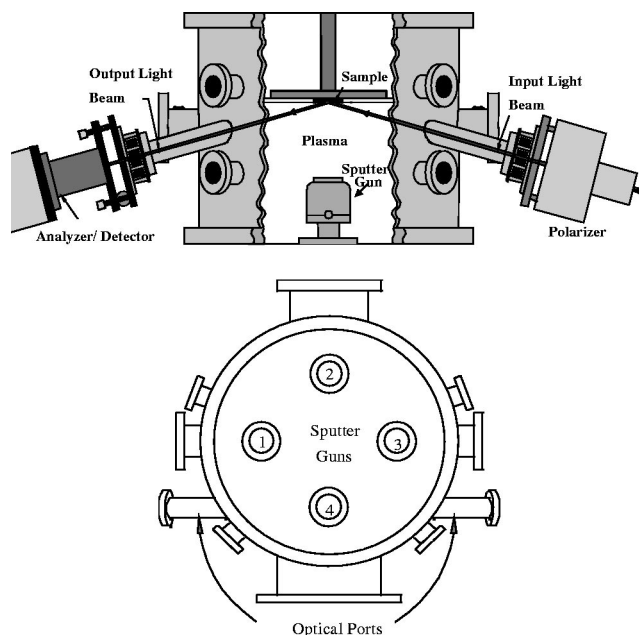


FIG. 1. Magnetron sputter gun in cryopumped vacuum deposition chamber.

sition was investigated at a sequence of gas pressures ranging from 2 to 5 mTorr, dc power of 35 W, and deposition durations of 20, 30, or 40 min. All films were optically thick. X-ray diffraction data of the as-deposited Ir films show a preferred (1 1 1) orientation, regardless of the deposition parameters employed.

### B. Film analysis

AFM was used to measure the rms surface microroughness under ambient conditions. Data were obtained over an area of  $2\ \mu\text{m} \times 2\ \mu\text{m}$  using a DI (Digital Instruments) AFM Dimension<sup>TM</sup> 3100 in the Tapping Mode.

Spectroscopic ellipsometry (SE) is a well-known surface sensitive, nondestructive optical technique widely used to determine film thickness and optical constants.<sup>17–20</sup> Reflection ellipsometry measures the change of polarization state of light upon reflection from a sample surface. Measurement results are expressed as psi ( $\Psi$ ) and delta ( $\Delta$ ), which are related to the complex Fresnel reflection coefficients ( $R$ ) by<sup>20</sup>

$$\rho \equiv \tan(\Psi)e^{i\Delta} = R_p/R_s, \quad (1)$$

where  $p$  and  $s$  correspond to electric field component directions parallel and perpendicular to the plane of incidence, respectively. In this work, the optical constants of the as-deposited Ir films were determined using variable angle spectroscopic ellipsometry. Measurements were performed over a wide spectral range, using two separate ellipsometers. The first covered the VUV to near-infrared (NIR) (140–1700 nm). The second was an infrared ellipsometer utilizing a rotating polarizer, rotating compensator configuration, with a spectral range of  $8000\text{--}250\ \text{cm}^{-1}$  ( $1.25\text{--}40\ \mu\text{m}$ ). All spectroscopic ellipsometry data were taken at three angles of incidence ( $50^\circ$ ,  $55^\circ$ ,  $60^\circ$ ). Detailed information on spectroscopic ellipsometric measurements can be found elsewhere.<sup>21</sup>

## III. RESULTS AND DISCUSSIONS

### A. Microroughness of the as-deposited Ir films

Initially, Ir films were deposited onto fused silica substrates directly, with no Cr layers underneath. These films spalled over the entire sample surfaces, likely due to residual stress between the substrate and the depositing film. These films were obviously not acceptable. Cr has long been used as an intermediate layer, to decrease residual stress and enhance film adhesion; so, it was an obvious material of choice in this study. With Cr buffer layers, the final Ir films were so smooth that optical microscopy was unable to detect anything other than clean, bright, mirror-like surfaces. The Ir smoothness and microstructure dependence on process parameters was determined for a series of samples using AFM. Table I lists six different samples prepared under six different deposition conditions.

At a dc power of 35 W and an Ar gas flow of 20 sccm, samples Nos. 1–4 (see Table I) were deposited at gas pressures ( $P$ ) of 5, 4, 3, and 2 mTorr, respectively. Shown in Fig. 2 is a general AFM image of Ir films deposited in this study. The rms roughness values calculated from AFM were only 0.84, 0.44, 0.41, 0.3 nm, respectively, suggesting that the films consisted of closely packed grains with very fine grain sizes. The average roughness decreased slightly with decreasing gas pressure. This was somewhat expected, because lower gas pressure reduced incident working gas (Ar) entrapment in the film, and increased sputtering particle energies (due to fewer collisions with the sputter inert gas) when they strike the substrate, resulting in better adhesion.<sup>22</sup>

TABLE I. A list of six Ir/Cr/fused silica samples prepared under different deposition conditions.

Sample No.	Ar flow (sccm)	dc power (W)	Pressure (mTorr)	Deposition time (min)	Thickness <sup>a</sup> (approx.) (nm)	rms roughness (nm)
1	20	35	5	20	240	0.84
2	20	35	4	20	240	0.44
3	20	35	3	20	240	0.41
4	20	35	2	20	240	0.3
5	20	35	5	30	360	1.0
6	20	35	5	40	480	1.03

<sup>a</sup>Thickness is calculated based on an approximate sputtering deposition rate of 0.2 nm/s, a typical value for metals.

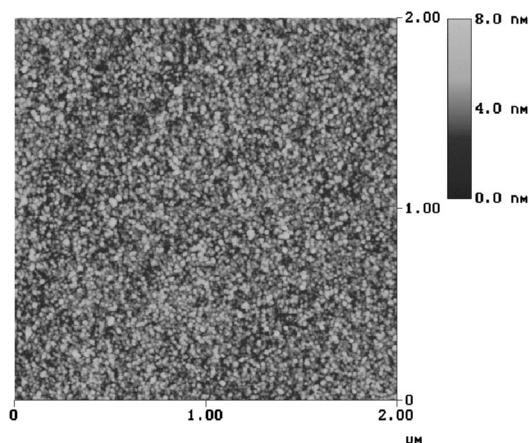


FIG. 2. Typical AFM image of Ir films deposited in this study.

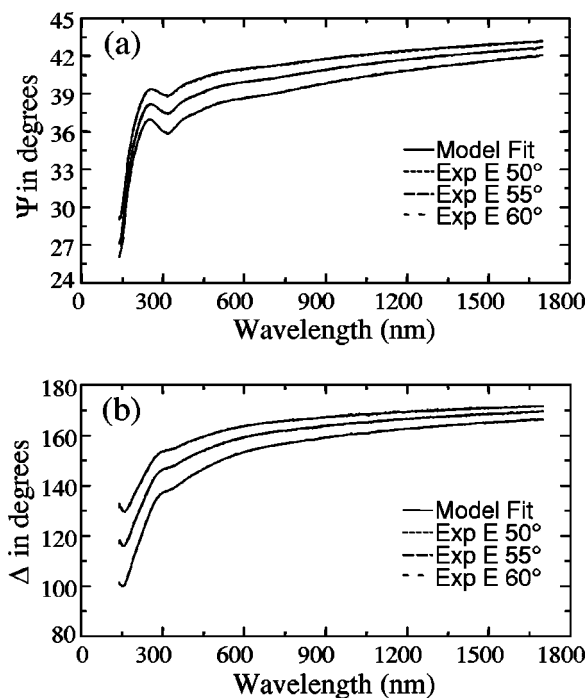
Film thickness (assumed to be linear with deposition time) had an important influence on film topography. At 35 W, 20 sccm Ar gas flow, and 5 mTorr gas pressure, Ir samples Nos. 1, 5, and 6 (see Table I) were sputter deposited for 20, 30, and 40 min, respectively. The rms roughness values were 0.84, 1.0, and 1.03 nm, respectively. Results show increasing roughness with increasing thickness. As our main goal was to prepare as smooth surfaces as possible, relatively thinner films were favored, yet they still had to be optically thick (thickness greater than 100 nm for metals). This was important because eventually we determined the optical constants on as-deposited films using spectroscopic ellipsometry and light reaching the backsurface would complicate ellipsometric analysis.

### B. Ir optical constants

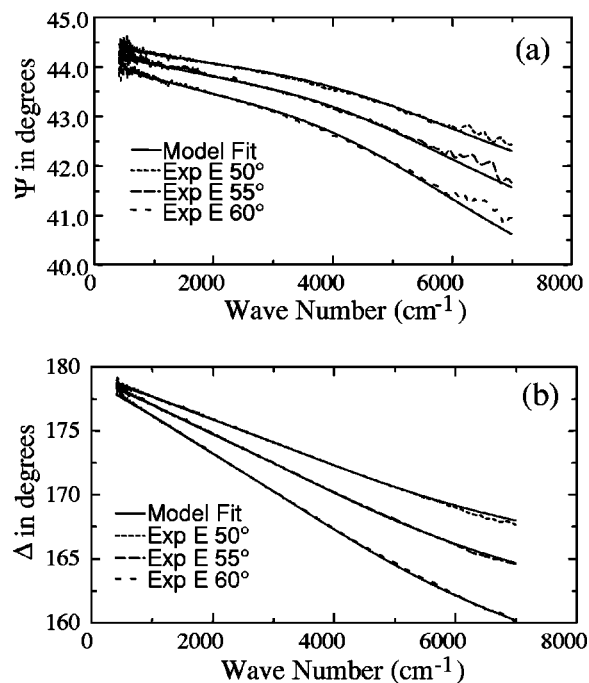
Figures 3 and 4 show typical VASE raw data ( $\psi$  and  $\Delta$ ) along with model fits for Ir/Cr/fused silica samples made in this study. Ellipsometers covering the VUV-visible-NIR (140–1700 nm) (Fig. 3), and the MIR (8000–250  $\text{cm}^{-1}$ ) (Fig. 4) were used.

Data were represented by a classical Drude dispersion layer along with a few Gaussian oscillators, to account for both free carrier absorption and interband absorption, in the optical model.<sup>20</sup> Surface roughness was modeled by a Bruggeman effective medium approximation layer using the rms thickness values taken directly from AFM results, assuming 50% material and 50% void. Because films were optically thick, the thicknesses of what were underneath, including both the fused silica substrate and the Cr adhesion layer, did not matter. Excellent fits were achieved, as shown in Figs. 3 and 4. Note that only one parametric model set was employed to cover the entire spectral range from the VUV to MIR.

As a general rule, film density increases with increasing film thickness until reaching bulk density where it saturates. The thickness at which a film density approaches its bulk value may vary, depending on the deposition technique as well as conditions. Optical constants for very thin films can be somewhat different than those of bulk metals. In this study, Ir metal films were deposited in an inert Ar gas atmo-

FIG. 3. Typical SE raw data obtained from the as-deposited Ir samples, combined with model fits, over the VUV-visible-NIR (140–1700 nm). (a)  $\psi$ . (b)  $\Delta$ .

sphere, at relatively low operating pressures, without heating the substrates (i.e., at room temperature), and long enough to be optically thick. As a result, the resulting films showed extremely clean, smooth surfaces (recall the small rms values from AFM). They were also free from oxides or contaminants, as evidenced by energy dispersive x-ray data (EDX) taken on the as-deposited Ir sample films, which showed the

FIG. 4. Typical SE raw data obtained from the as-deposited Ir samples, combined with model fits, over the MIR (8000–250  $\text{cm}^{-1}$ ). (a)  $\psi$ . (b)  $\Delta$ .

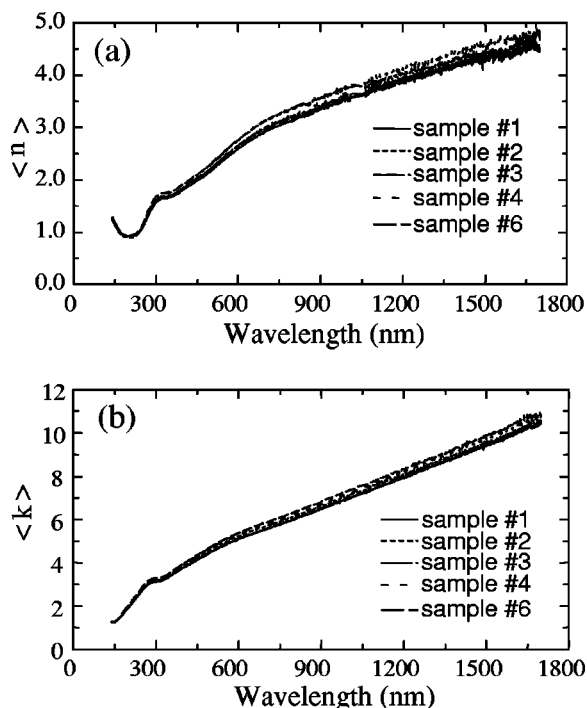


FIG. 5. Comparison of SE raw data ( $60^\circ$ ) taken on five different samples (sample Nos. 1, 2, 3, 4, and 6, see Table I) in the VUV-visible-NIR. (a)  $\langle n \rangle$ . (b)  $\langle k \rangle$ .

Ir peak with nothing else. Thus, the optical constants acquired from these films are representative of Ir bulk metals.

Shown in Figs. 5 and 6 are comparisons of SE raw data taken on five different samples (see Table I), over the VUV-visible-NIR and MIR, respectively. For clarity purpose, only

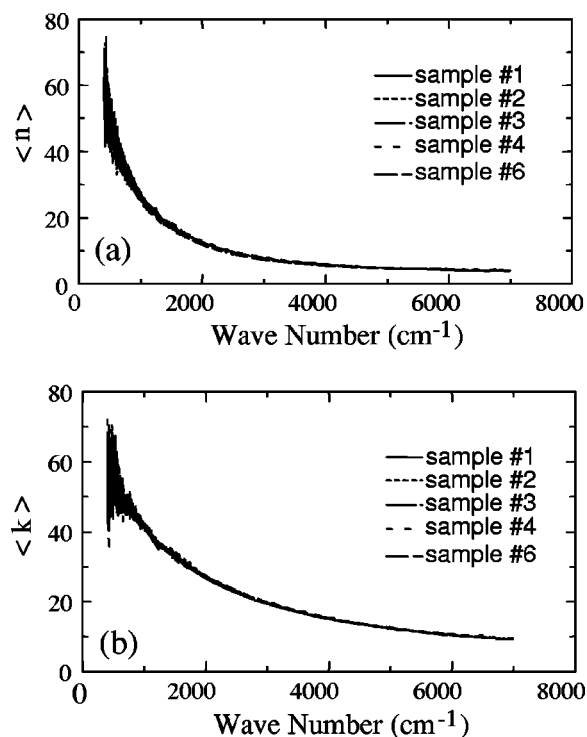


FIG. 6. Comparison of SE raw data ( $60^\circ$ ) taken on five different samples (sample Nos. 1, 2, 3, 4, and 6, see Table I) in the MIR. (a)  $\langle n \rangle$ . (b)  $\langle k \rangle$ .

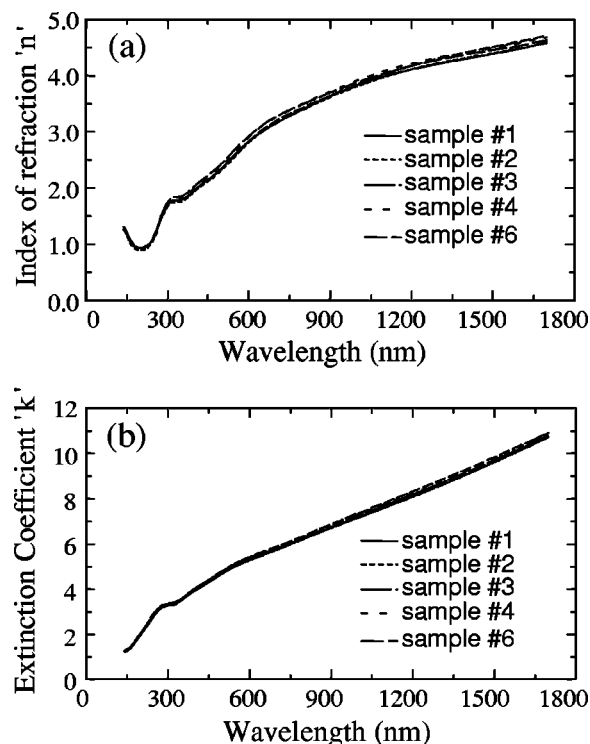


FIG. 7. Ir film optical constants obtained from five different samples (sample Nos. 1, 2, 3, 4, and 6, see Table I) in the VUV-visible-NIR (140–1700 nm). (a)  $n$ . (b)  $k$ .

data taken at  $60^\circ$  are displayed. The data are expressed in terms of pseudo-optical constants  $\langle n \rangle$  and  $\langle k \rangle$ , as a visual way of comparing “raw data.” Theoretically, unless determined on a smooth, nonmultilayered surface, the pseudo-optical constants thus obtained would not be characteristic of the true sample structure.<sup>20,23</sup> However, plotting the pseudo-optical constants is a good indicator of how the film topography (surface roughness, specifically) affects the raw data. The Ir optical constants ( $n$  and  $k$ ) determined from these five samples are shown in Figs. 7 and 8, over the VUV-visible-NIR and the MIR, respectively. Despite slight differences, they are indeed very close to each other.  $n$  (and  $k$ )’s are virtually lying on top of each other with only slight deviations, mainly seen in the lower wavelength spectral range. No appreciable differences among samples were detected in the MIR, as shown in Fig. 8. This indicates the low scattering of infrared light by roughness, and further justifies the fact that these films are optically thick and the optical constants correspond to bulk values. Note that these optical constants differ slightly from the pseudo-optical constants (as shown in Figs. 5 and 6). By modeling we remove the effects of surface roughness, and therefore determine the true optical constants of the metal; as a result, there should not be any differences in the optical constants among samples. The slight deviations, mainly seen in Fig. 7, are likely due to the fact that AFM and optical spectra do not measure quite the same “roughness.”

Ir optical constants provided by other sources, taken on different sample forms (either bulk or thin films), and under different ambient conditions, can be found in the literature—Palik’s handbook in particular.<sup>15,16</sup> There are significant dif-



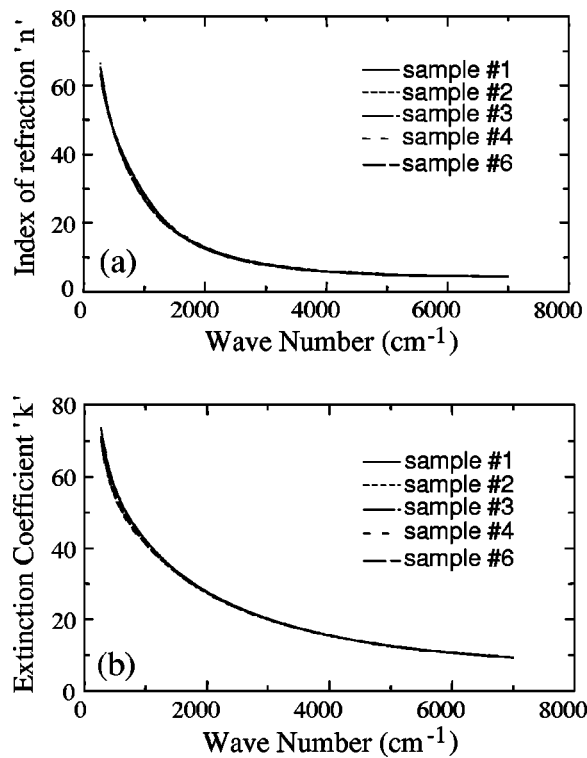


FIG. 8. Ir film optical constants obtained from five different samples (sample Nos. 1, 2, 3, 4, and 6, see Table I) in the MIR (8000–250  $\text{cm}^{-1}$ ). (a)  $n$ . (b)  $k$ .

ferences or inconsistencies, which are likely due to different surface roughnesses on samples evaluated in each case. Qualitatively, Palik's Ir optical constants agree with ours fairly well; quantitatively, however, they have lower values in both  $n$  and  $k$ , which, generally, suggests an unaccounted surface roughness. A simulation was thereof conducted to see if this was the case here. By adding  $\sim 4.1$  nm surface roughness, we were able to match Palik's values based on our reported optical constants. In view of all of this, we believe the present work represents the best optical constants available for intrinsic Ir material, and cover the widest spectral range. Listed in Table II are the as-determined Ir optical constants at a few selected wavelengths. (There are slight differences among the five samples studied, and the optical constants for sample No. 2 were presented in Table II since they are the ones lying in between.)

### C. Roughness and overlayer affects on apparent optical constants

Simulations of surface overlayer (both roughness and potential hydrocarbons adsorbed onto the sample surfaces) effects on Ir film optical constants,  $n$  and  $k$ , were performed using the analysis software. These were based on the acquired true Ir optical constants discussed earlier in this article, and done by adding the overlayers explicitly in the optical model. Figure 9 shows variations of calculated  $n$  and  $k$  due to a change in roughness layer thickness, assuming it to be 0, 0.5, 1, and 1.5 nm, respectively. Clearly, the roughness effects on Ir film optical constants are substantial; major

TABLE II. Ir optical constants at selected wavelengths.

eV	$n$	$k$
8.857	1.25	1.23
8.493	1.19	1.24
7.949	1.08	1.32
7.294	0.96	1.52
6.739	0.90	1.75
6.263	0.89	1.98
5.794	0.90	2.25
5.254	0.98	2.65
4.882	1.14	2.96
4.429	1.48	3.23
4.026	1.72	3.31
3.584	1.76	3.50
3.1	1.93	3.98
2.719	2.14	4.39
2.5	2.30	4.70
2.206	2.63	5.15
2	2.89	5.44
1.908	3.00	5.58
1.797	3.12	5.76
1.699	3.23	5.94
1.602	3.33	6.15
1.501	3.45	6.40
1.403	3.57	6.69
1.302	3.71	7.02
1.202	3.86	7.40
1.101	4.01	7.84
1.01	4.14	8.32
0.901	4.29	9.05
0.8	4.44	9.97
0.701	4.65	11.21
0.602	5.03	12.91
0.501	5.78	15.37
0.4	7.25	18.79
0.3	10.11	23.74
0.25	12.53	27.18
0.2	16.19	31.65
0.15	22.32	37.58
0.1	32.83	45.20
0.095	34.29	46.18
0.08	38.94	49.31
0.07	42.66	51.91
0.06	47.04	55.15
0.05	52.29	59.29
0.04	59.28	65.17
0.034	64.96	70.17

shifts in  $n$  and  $k$  are observed due to tenths of a nanometer changes in roughness. Notice also increasing roughness decreases both  $n$  and  $k$ .

Likewise, another simulation was made of hydrocarbon overlayer effects on Ir film optical constants, as illustrated in Fig. 10. Polyethylene (PE), a common hydrocarbon, was employed to account for the possible hydrocarbon overlayers present, with a thickness of 0, 0.5, 1, and 1.5 nm, respectively. As can be seen, the changes in  $n$  and  $k$  are similar to changes due to surface roughness, as shown in Fig. 9.

Overall, Ir film optical constants determination is very sensitive to surface overlayers, including surface roughness and possible adsorbed hydrocarbons. With that in mind, care must be exercised by future users if they are to employ our reported Ir optical constants. If possible, potential contamination and roughness need to be removed physically or ac-

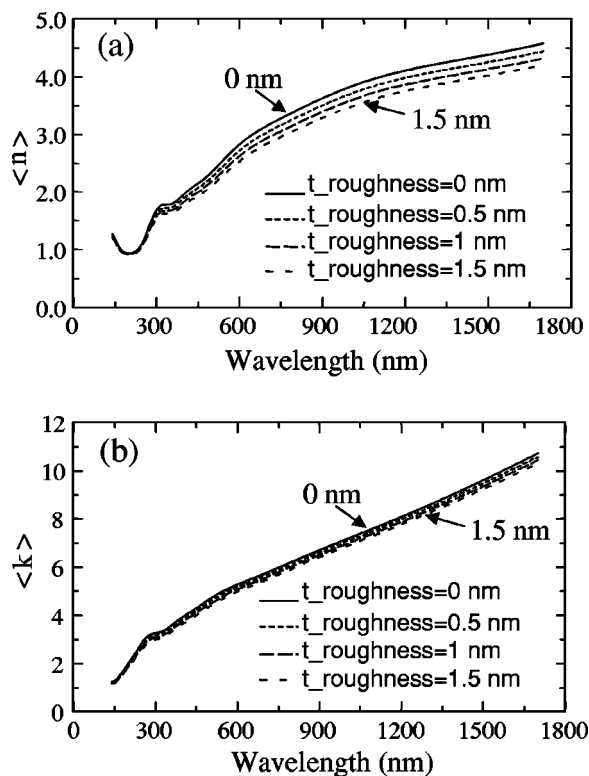


FIG. 9. A simulation of surface roughness effects on Ir film optical constants ( $n$  and  $k$ ), assuming the roughness thickness is 0, 0.5, 1, and 1.5 nm, respectively. (a)  $n$ . (b)  $k$ .

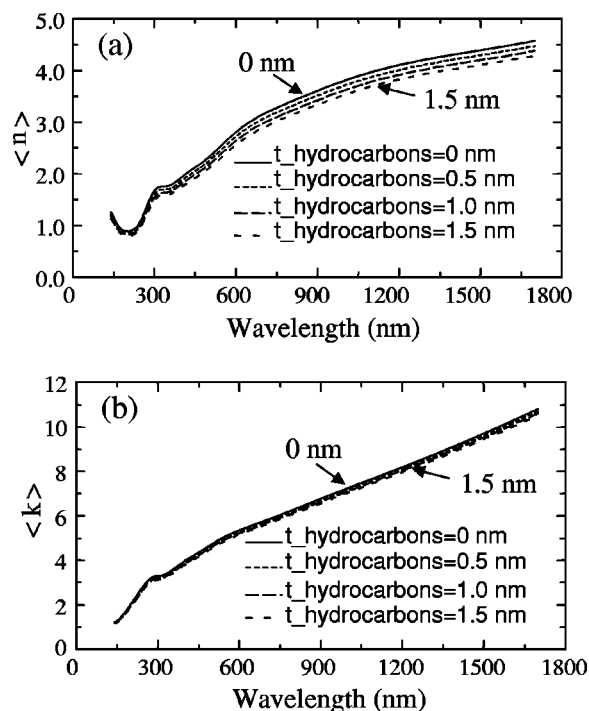


FIG. 10. A simulation of hydrocarbon overlayer effects on Ir film optical constants ( $n$  and  $k$ ), assuming the hydrocarbon is PE and its thickness is 0, 0.5, 1, and 1.5 nm, respectively. (a)  $n$ . (b)  $k$ .

counted for in the optical modeling. For space applications (such as the PEACE experiments),<sup>5,6</sup> these simulations show that Ir provides a highly sensitive base for detecting contamination.

#### IV. CONCLUSION

Ir films with extremely smooth surfaces ( $\text{rms} < 1$  nm, for most cases) were deposited by dc magnetron sputtering onto fused silica substrates at room temperature. Cr was employed as an intermediate layer, which improved adhesion between films and substrates. Surface morphologies and microstructures were examined under various conditions of gas pressure and deposition duration, using optical microscopy, AFM, x-ray diffraction, and EDX. Results indicate that, the average surface roughness decreased slightly with decreasing gas pressure in the chamber, and increased as a function of increased film thickness.

Variable angle spectroscopic ellipsometry was employed to determine Ir film optical constants from VUV through the middle IR (140 nm–35  $\mu\text{m}$ ). Because the Ir films were optically thick and the surface roughnesses were measured by AFM then accounted for in the optical model, the as-determined film optical constants are expected to be the best available for Ir bulk metals, minimally affected by surface overlayers or microstructure.

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